

① 次の公式を証明せよ.

$$(1) \cos \alpha \sin \beta = \frac{1}{2} \{ \sin(\alpha + \beta) - \sin(\alpha - \beta) \}$$

$$(2) \sin \alpha \sin \beta = -\frac{1}{2} \{ \cos(\alpha + \beta) - \cos(\alpha - \beta) \}$$

② 次の不定積分を計算せよ.

$$(1) \int \cos 4x \sin 2x \, dx$$

$$(8) \int \tan x \, dx$$

$$(2) \int \sin 8x \sin 3x \, dx$$

$$(9) \int \tan^2 x \, dx$$

$$(3) \int \sin^2 \frac{1}{2} x \, dx$$

$$(10) \int \sin^2 2x \, dx$$

$$(4) \int \sin 2x \cos 2x \, dx$$

$$(11) \int \cos^3 x \, dx$$

$$(5) \int x \cos x^2 \sin 2x^2 \, dx$$

$$(12) \int \sin^4 x \, dx$$

$$(6) \int \frac{1}{\cos^2 5x} \, dx$$

$$(13) \int \frac{1}{\cos 3x} \, dx$$

$$(7) \int \frac{x}{\sin^2 x^2} \, dx$$